

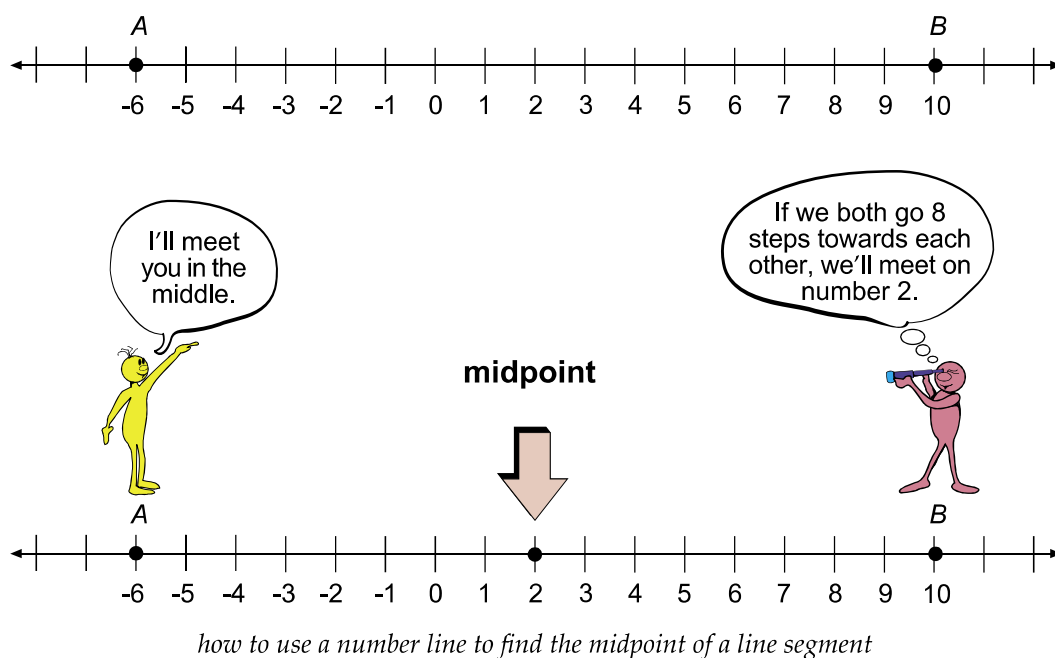
## Midpoint

Sometimes it is necessary to find the *point* that is exactly in the middle of two given **endpoints**. We call this the **midpoint (of a line segment)**. What we are actually trying to find are the **coordinates** of that point, which is like the *address* of the point, or its *location* on a coordinate plane or a **number line**.

### Finding the Midpoint of a Line Segment Using a Number Line

You can find the *midpoint* of a **line segment** ( $\text{—}$ ), also called a *segment*, in a couple of different ways. One way is to use a *number line*.

On a number line, you can find the midpoint of a *line segment* by counting in from both *endpoints* until you reach the middle.

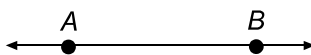




**Remember:** If we draw a *line segment* from one point to another, we can call it line segment  $\overline{AB}$  or *segment*  $AB$ . See a representation of line segment  $AB$  ( $\overline{AB}$ ) below. The symbol ( $\overline{\quad}$ ) drawn over the two uppercase letters describes a line segment. The symbol has no arrow because the line segment has a definite beginning and end called endpoints.  $A$  and  $B$  are endpoints of the line segment  $AB$  ( $\overline{AB}$ ).



On the other hand, the symbol ( $\longleftrightarrow$ ) drawn over two uppercase letters describes a line. The symbol has arrows because a line has no definite beginning or end.  $A$  and  $B$  are points on the line  $AB$  ( $\longleftrightarrow$ ).



## Method One Midpoint Formula

Another way to find the midpoint of a line segment is to use the Method One midpoint formula below. To do this, add the two endpoints together and divide by two.

**Method One midpoint formula**

$$\frac{a + b}{2}$$

$$\begin{aligned}\frac{a + b}{2} &= \\ \frac{-6 + 10}{2} &= \\ \frac{4}{2} &= \\ 2\end{aligned}$$



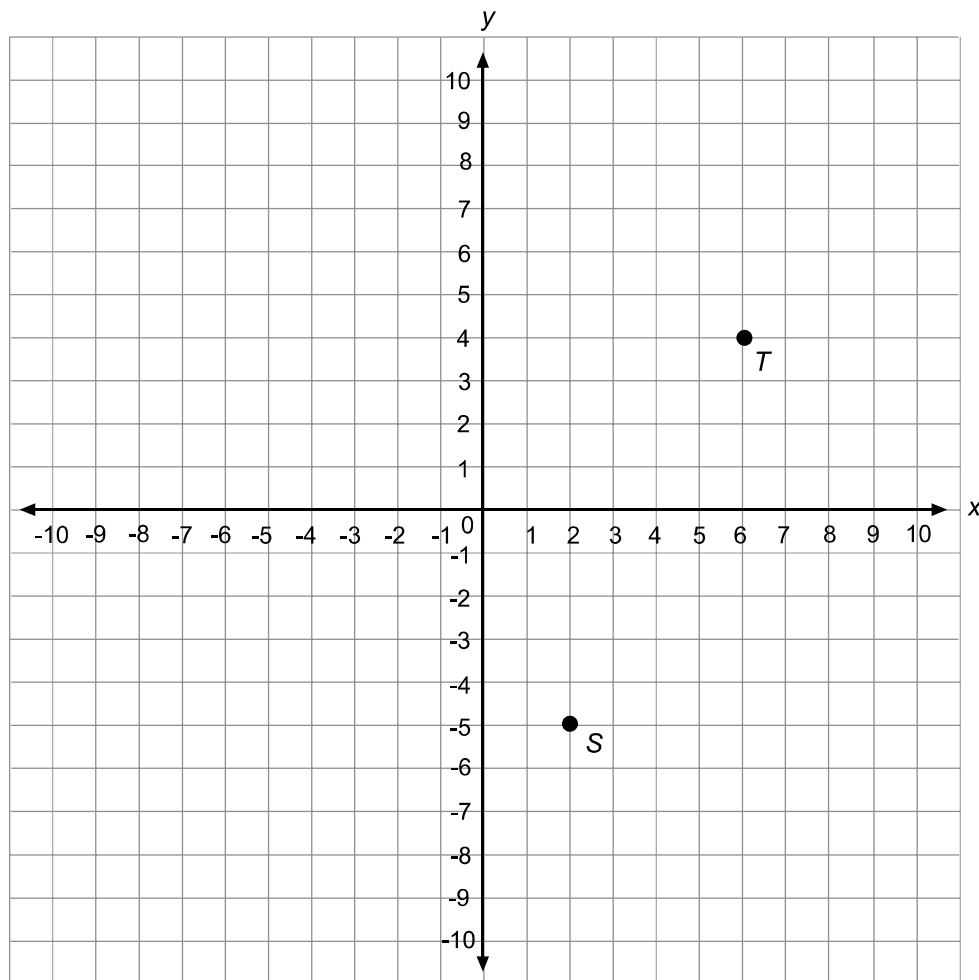
Therefore, for points  $A$  and  $B$  on the number line, the midpoint is

$$\frac{-6 + 10}{2} = \frac{4}{2} = 2.$$

## Method Two Midpoint Formula

Do you think the process may change a bit when we try to find the midpoint of points  $S$  and  $T$  as seen on the graph below?

Graph of Points  $S$  and  $T$



When the points are on a **coordinate plane**, or the plane containing the  $x$ - and  $y$ -axes, we have to think in two dimensions to find the *coordinates* of the midpoint. The midpoint will have an  **$x$ -coordinate** and a  **$y$ -coordinate** ( $x, y$ ). To find the midpoint on a coordinate plane, we simply use the Method Two midpoint formula twice—once to find the  $x$ -coordinate and again to find the  $y$ -coordinate.

### Method Two midpoint formula

$$\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Let's see how this works.

We see that point  $S$  has coordinates  $(2, -5)$ , and  $T$  is located at  $(6, 4)$ .  
Use the Method Two midpoint formula to find the exact location of the midpoint of  $\overline{ST}$ .

$$\begin{aligned} \text{midpoint of } \overline{ST} &= \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = && \begin{array}{l} \nearrow \text{find the } \textit{average} \text{ of the} \\ \searrow \text{x-values, then the average of} \\ \text{the y-values} \end{array} \\ &= \left( \frac{2+6}{2}, \frac{-5+4}{2} \right) = && \begin{array}{l} \nearrow \text{add the x's then the y's} \\ \searrow \end{array} \\ &= \left( \frac{8}{2}, \frac{-1}{2} \right) = && \begin{array}{l} \nearrow \text{now } \mathbf{simplify} \text{ each fraction} \\ \searrow \end{array} \\ &= \left( 4, \frac{-1}{2} \right) = \end{aligned}$$